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# The Mathematical Gazette

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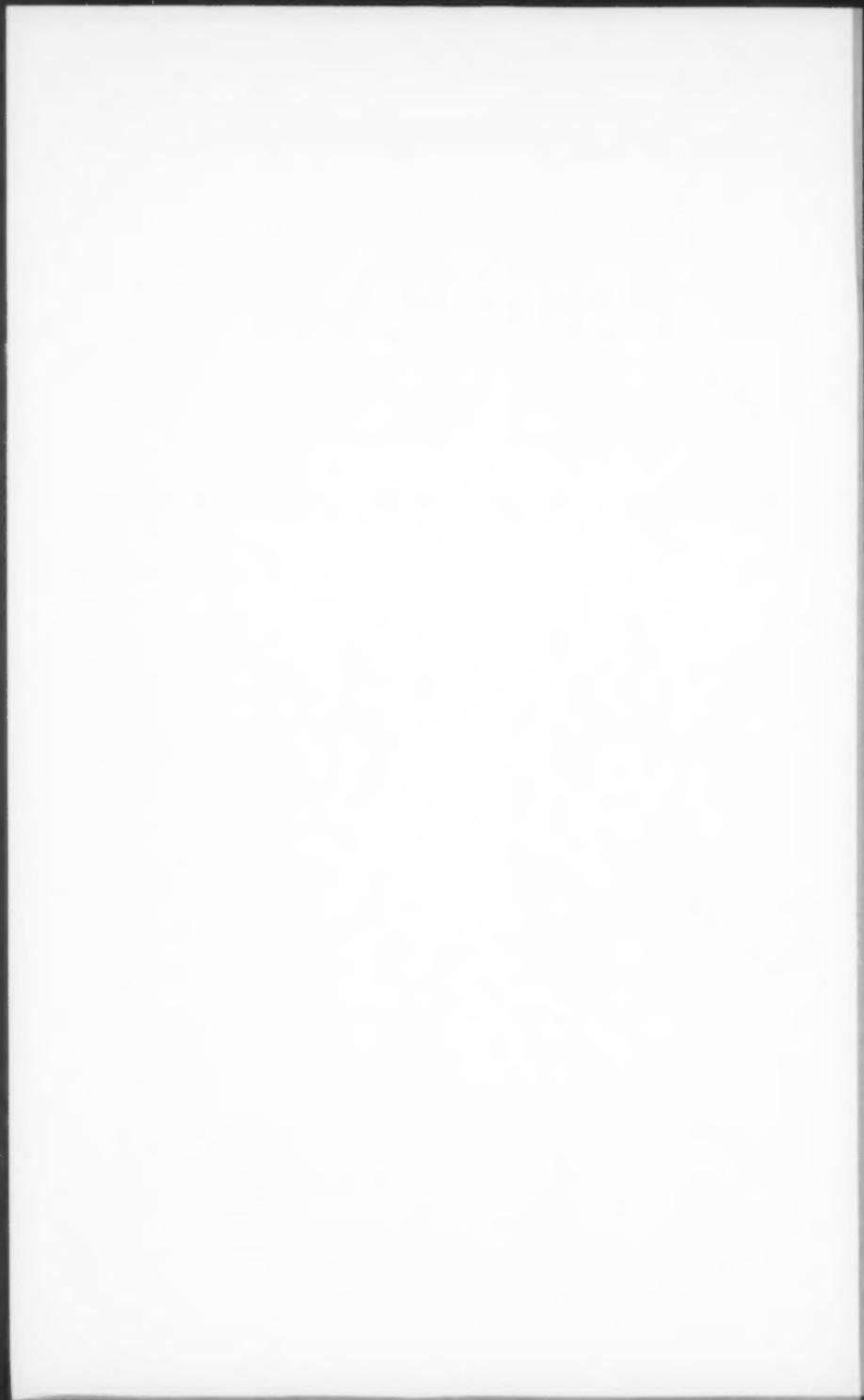
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THE MATHEMATICAL ASSOCIATION

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Vol. 90

2006

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**The 2006 *Gazette* editorial team**

<i>Editor</i>	Dr Gerry Leversha
<i>Production Editor</i>	Mr Bill Richardson
<i>Reviews Editor</i>	Mr Hugh Williams
<i>Problem Corner Editor</i>	Mr Nick Lord
<i>Student Problem Corner</i>	Mr Tim Cross
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<i>Proofreaders</i>	Mr Keith Barnett, Mr Colin Davis, Mr Michael Fox

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